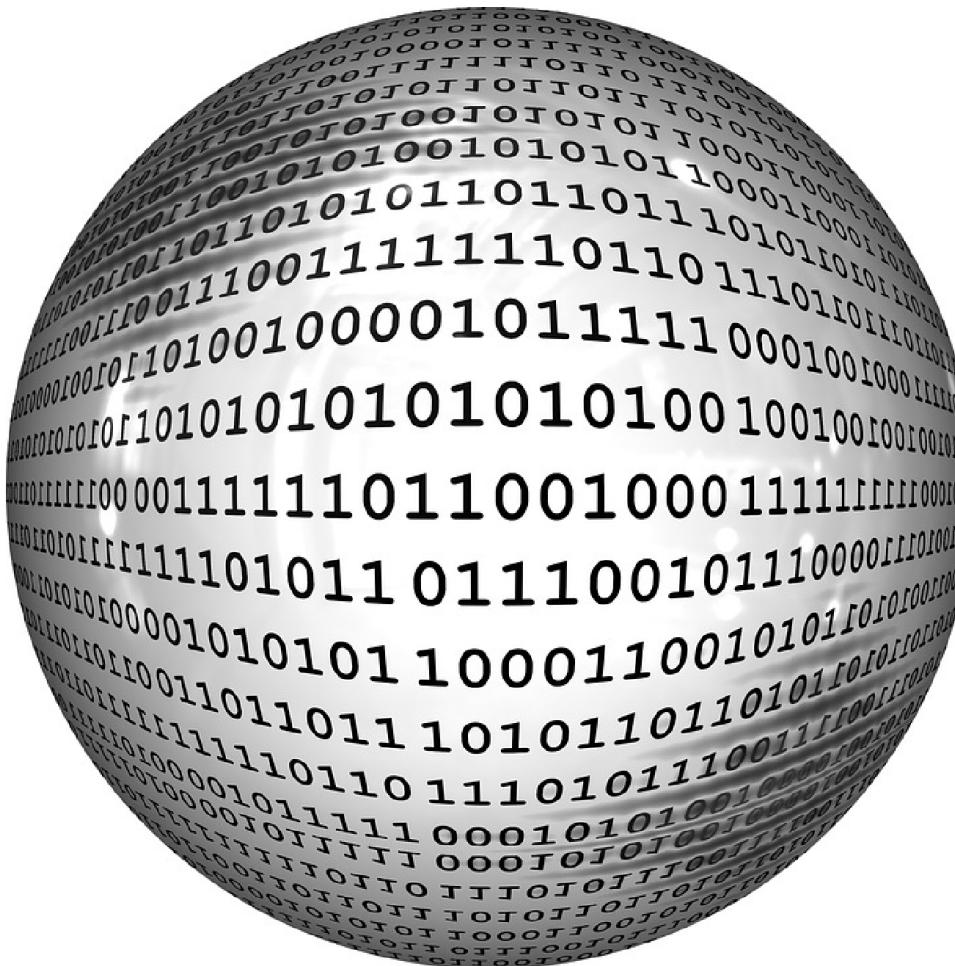


# Bitwise operators



# Reading list

- Read Kernighan & Ritchie Page 48-49
- Lecture Slides
- Reading material from the course website

A2+B2: Lab exam (online) after  
midterm break

# Most Commonly Used Laws of Operators

$$a \& 0 \rightarrow 0$$

$$a \& 1 \rightarrow a$$

$$a \& a \rightarrow a$$

$$a | 0 \rightarrow a$$

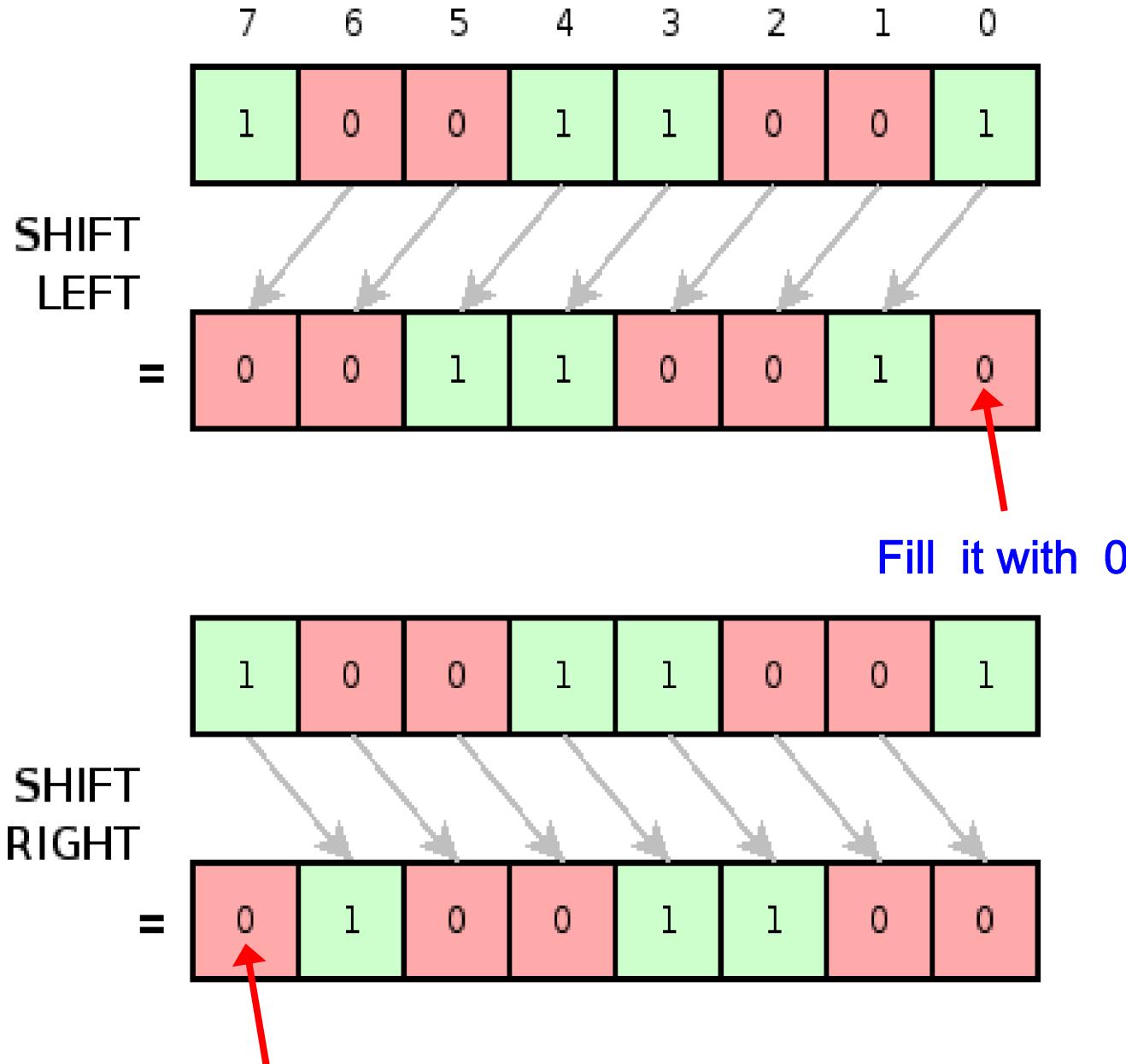
$$a | 1 \rightarrow 1$$

$$a | a \rightarrow a$$

$$a ^ 0 \rightarrow a$$

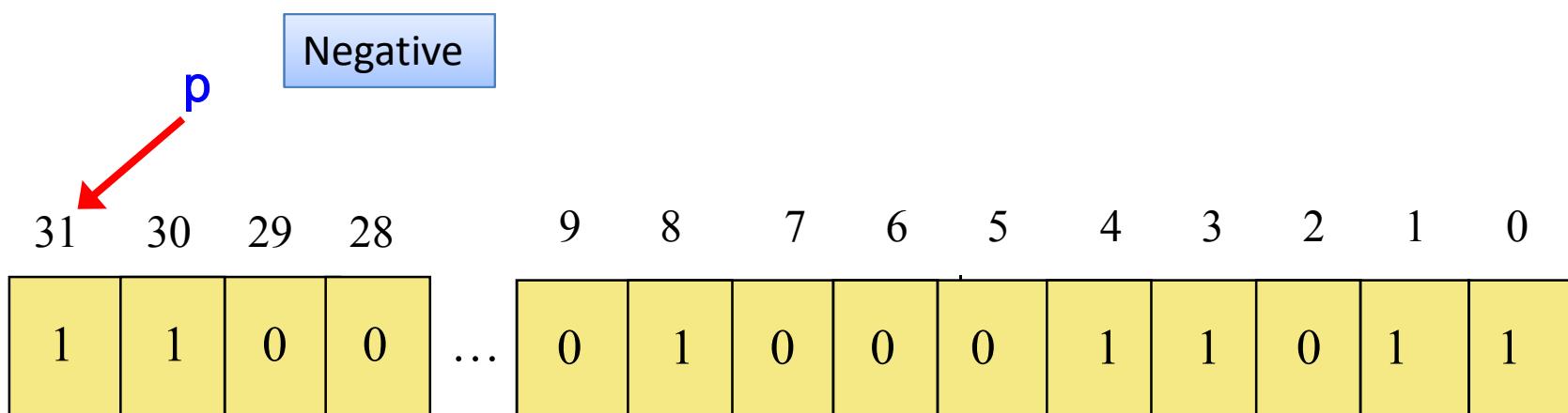
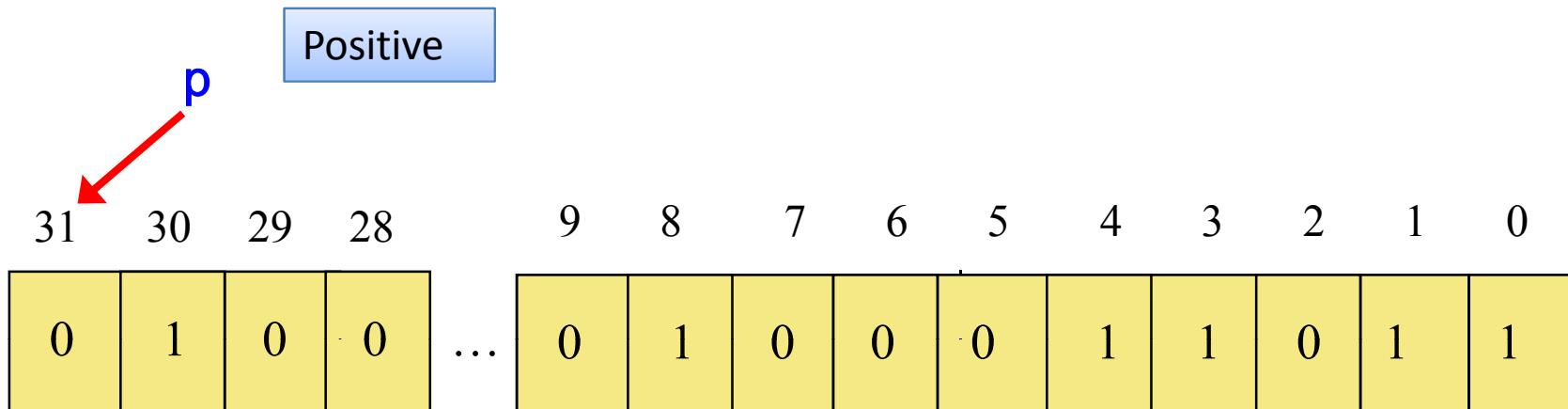
$$a ^ 1 \rightarrow \sim a$$

$$a ^ a \rightarrow 0$$



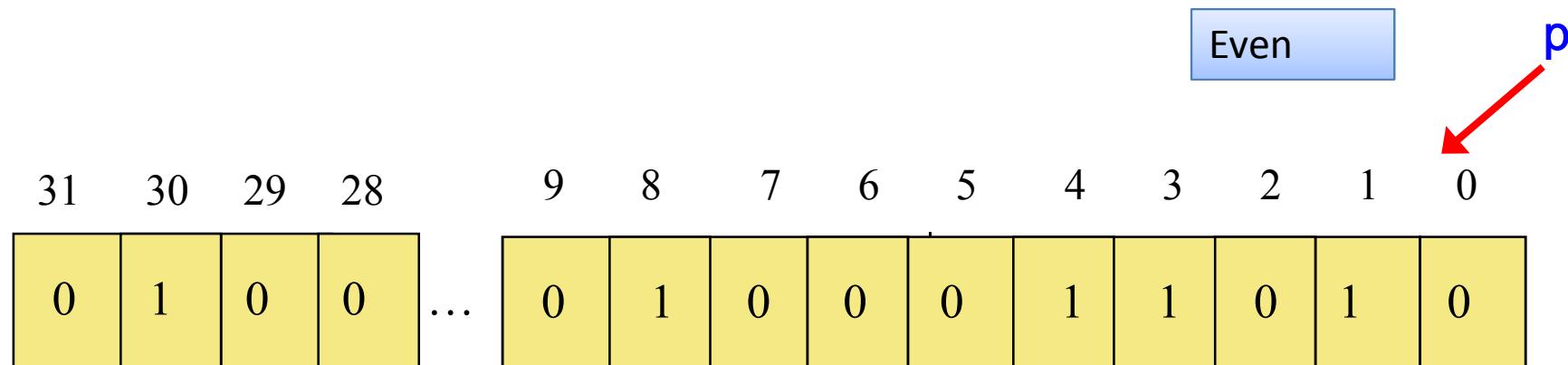
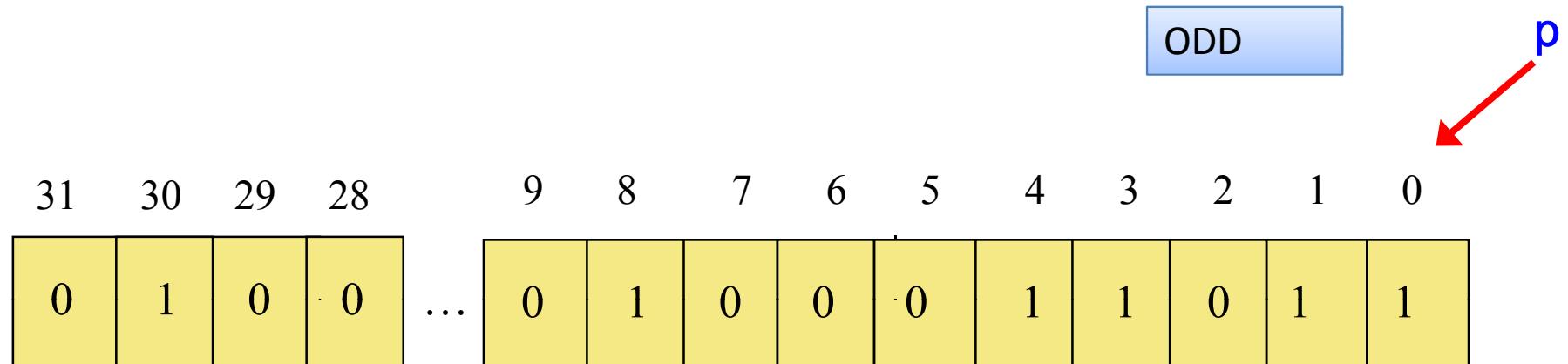
# Some quick examples

Determining a number positive or negative?



# Some quick examples

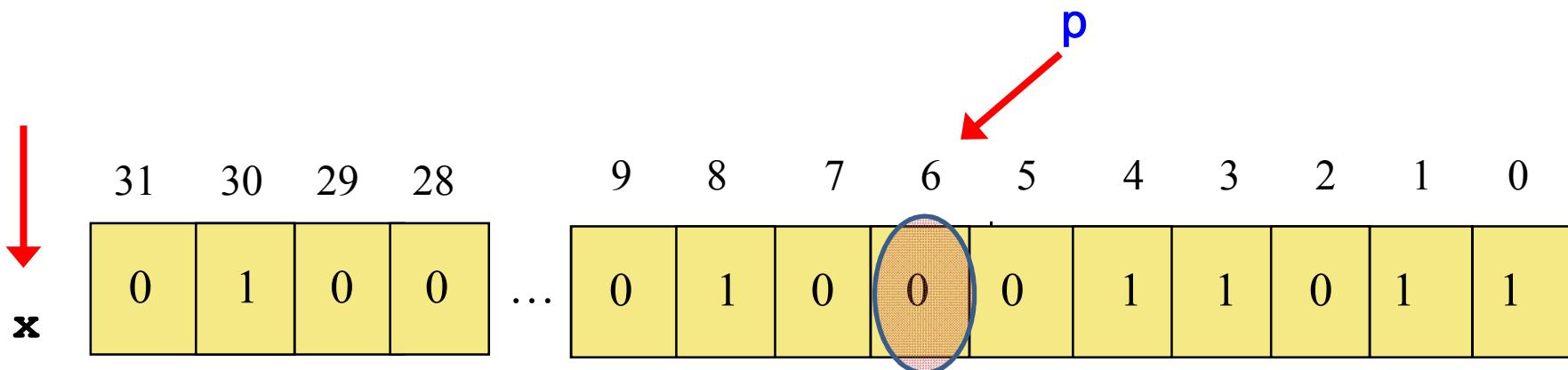
Determining a number odd or even?



# $\text{setBit}(x, p)$

Write down a function  $\text{setBit}(x, p)$  that will **set** a bit of integer  $x$  at position  $p$  leaving other bits unchanged.

Assume  $0 \leq p \leq 31$

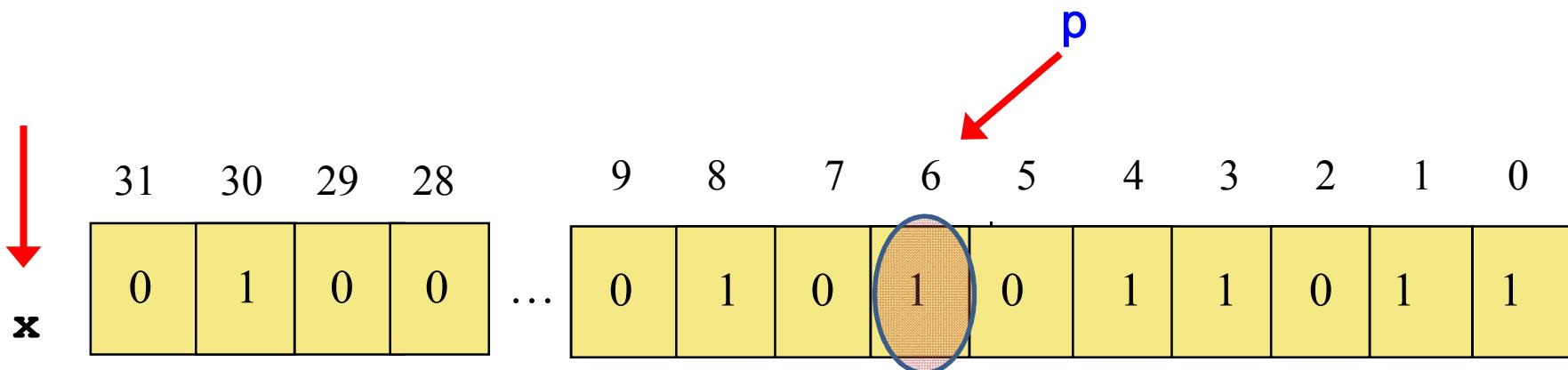


$\text{setBit}(x, 6)$

# $\text{setBit}(x, p)$

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$\text{setBit}(x, 6)$

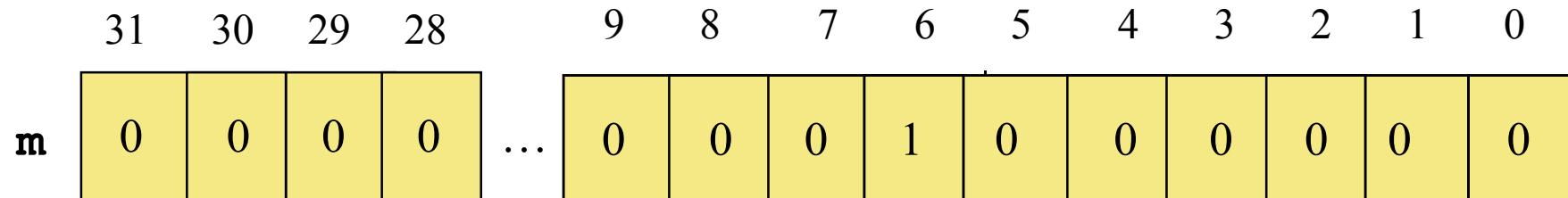
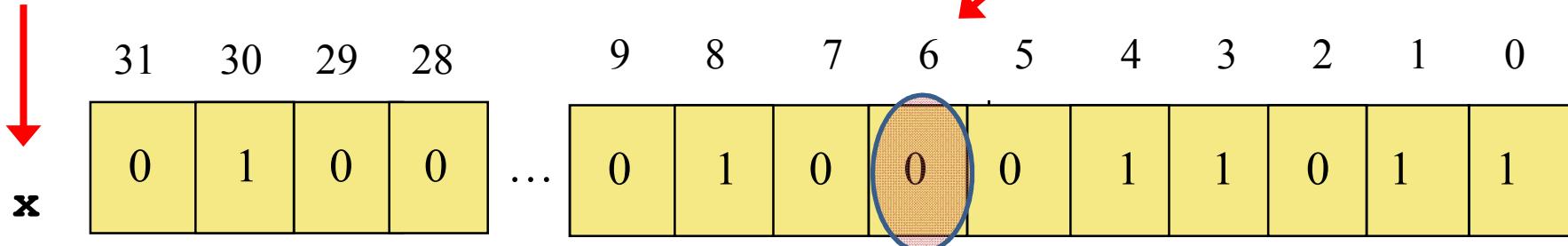
a   0	$\rightarrow$	a
a   1	$\rightarrow$	1
a   a	$\rightarrow$	a

setBit(x,p)

Write down a function setBit(x,p) that will **set** a bit of integer x at position p leaving other bits unchanged.

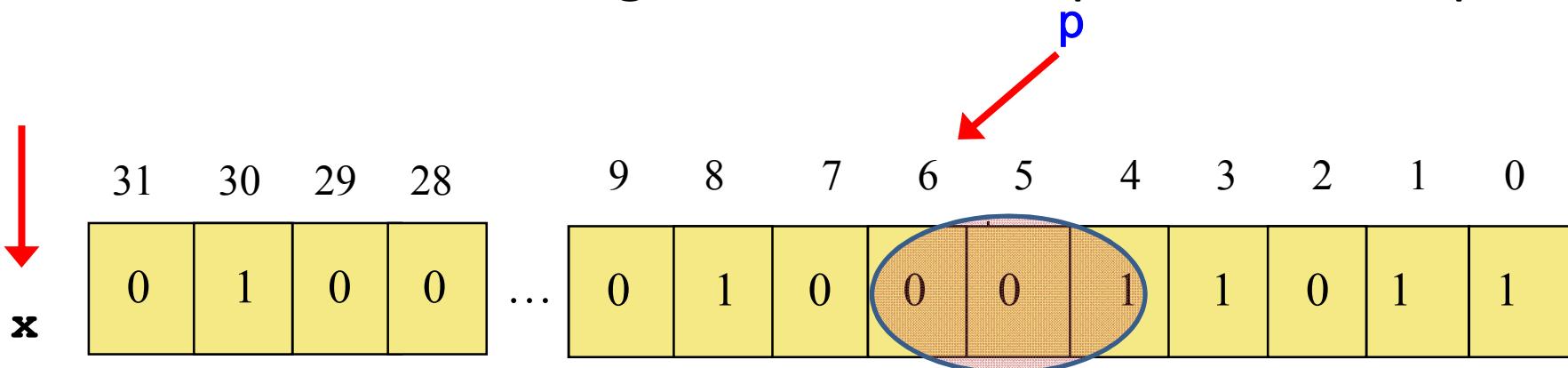
Assume  $0 \leq p \leq 31$

setBit(x, 6)



# $\text{setBits}(x, p, n)$

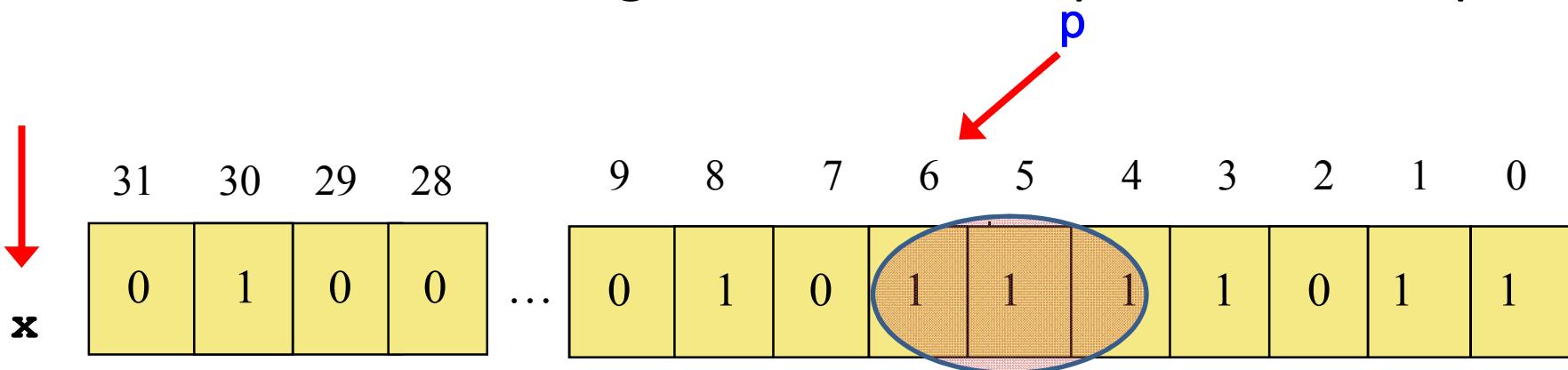
Write down a function  $\text{setBits}(x, p, n)$  that will **set** the  $n$  bits of the integer  $x$  starting from position  $p$  leaving other bits unchanged. Assume  $0 \leq p \leq 31$  and  $n \leq p+1$



$\text{setBits}(x, 6, 3)$

# $\text{setBits}(x, p, n)$

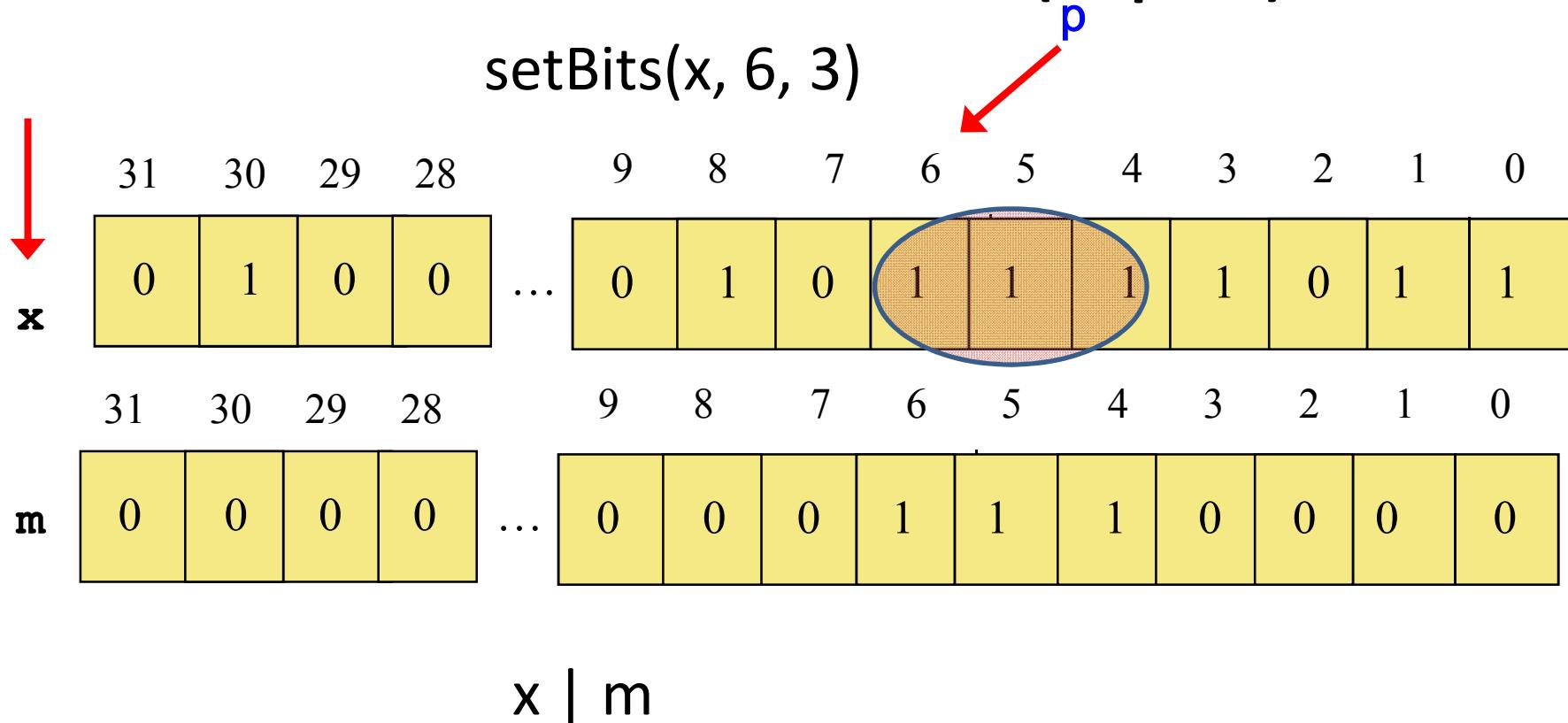
Write down a function  $\text{setBits}(x, p, n)$  that will **set** the  $n$  bits of the integer  $x$  starting from position  $p$  leaving other bits unchanged. Assume  $0 \leq p \leq 31$  and  $n \leq p+1$



$\text{setBits}(x, 6, 3)$

Call  $\text{setBit}(x, p)$  in a loop

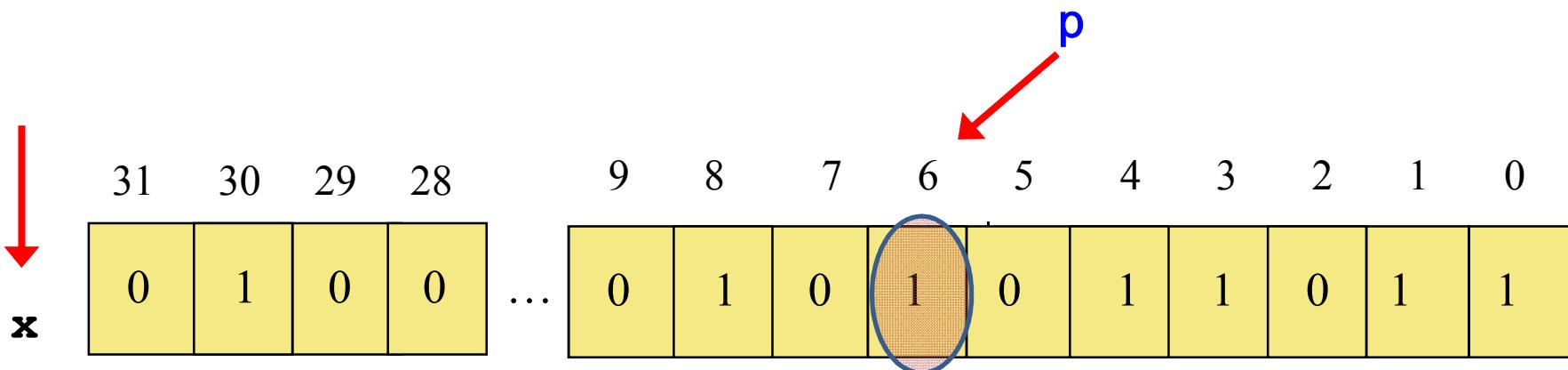
# Efficient setBits(x, p, n)



# $\text{resetBit}(x, p)$

Write down a function  $\text{resetBit}(x, p)$  that will **reset** a bit of integer  $x$  at position  $p$  leaving other bits unchanged.

Assume  $0 \leq p \leq 31$

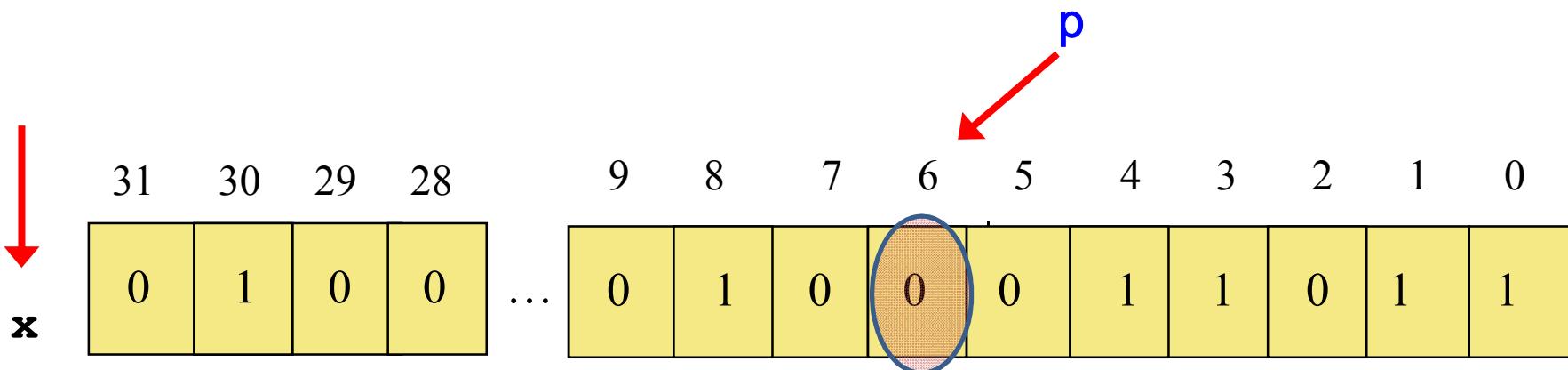


$\text{resetBit}(x, 6)$

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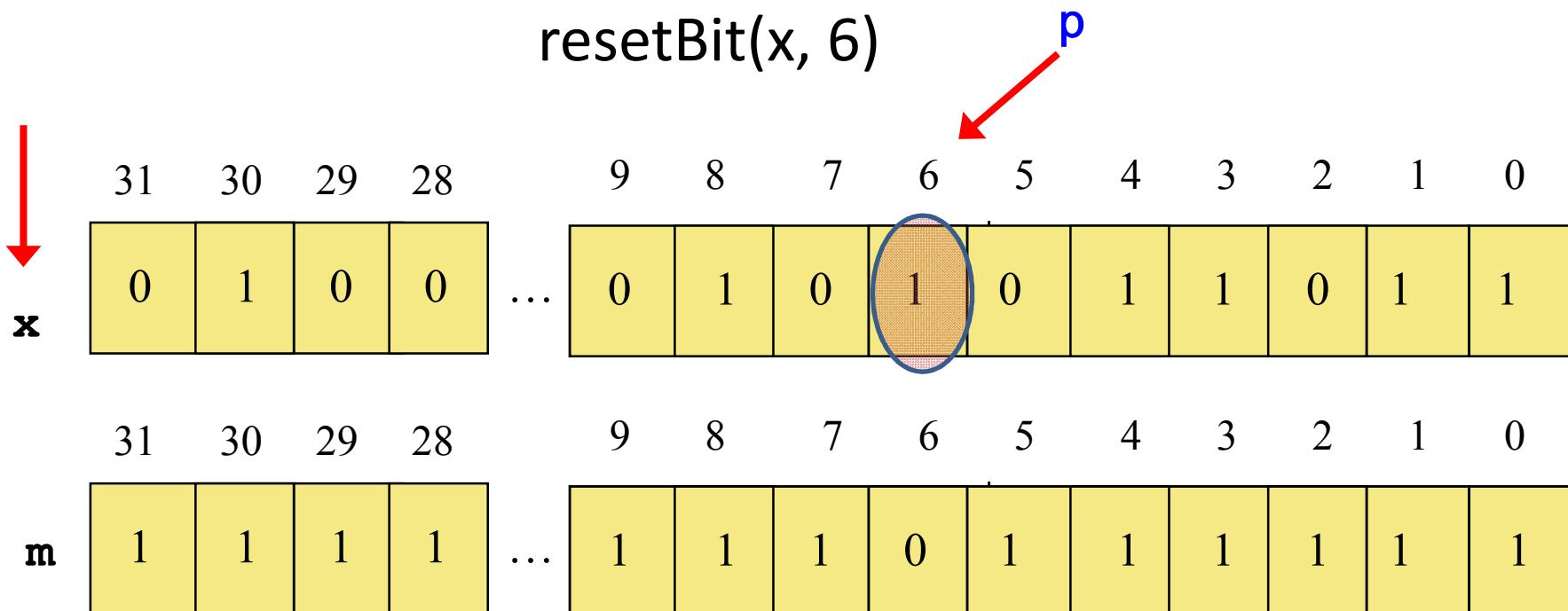
$\text{resetBit}(x, 6)$

$a \& 0 \rightarrow 0$
$a \& 1 \rightarrow a$
$a \& a \rightarrow a$

# resetBit(x,p)

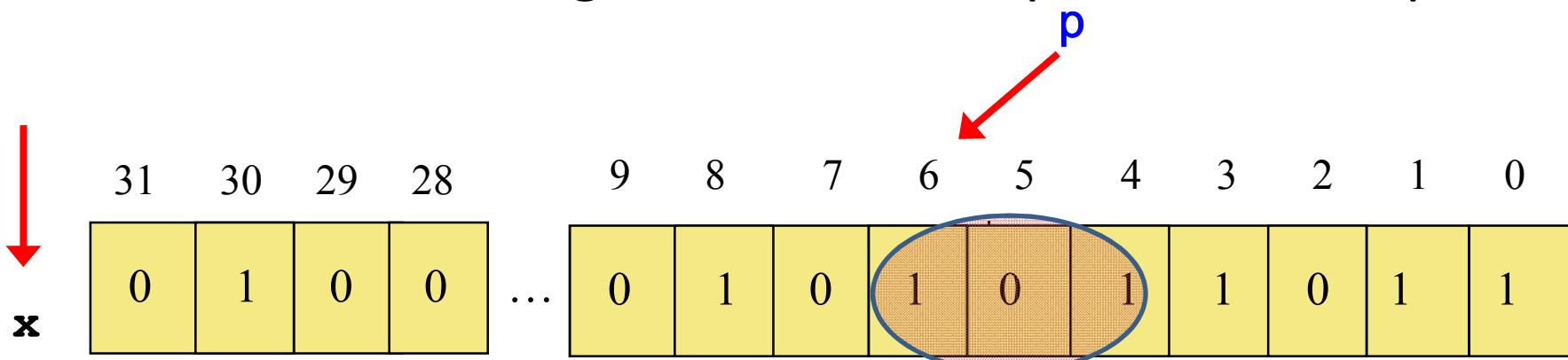
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Assume  $0 \leq p \leq 31$



# resetBits(x,p,n)

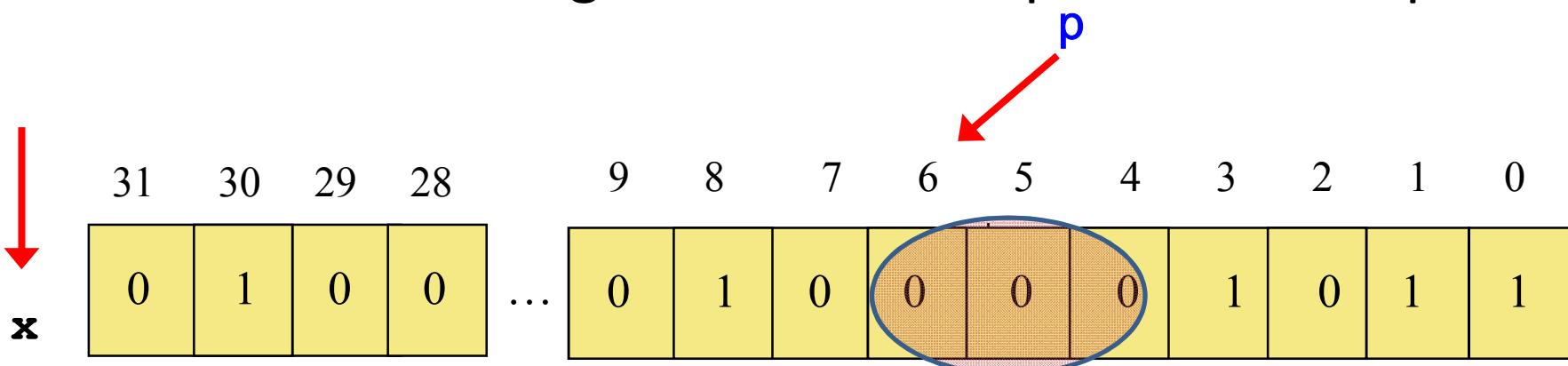
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$\text{resetBits}(x, 6, 3)$

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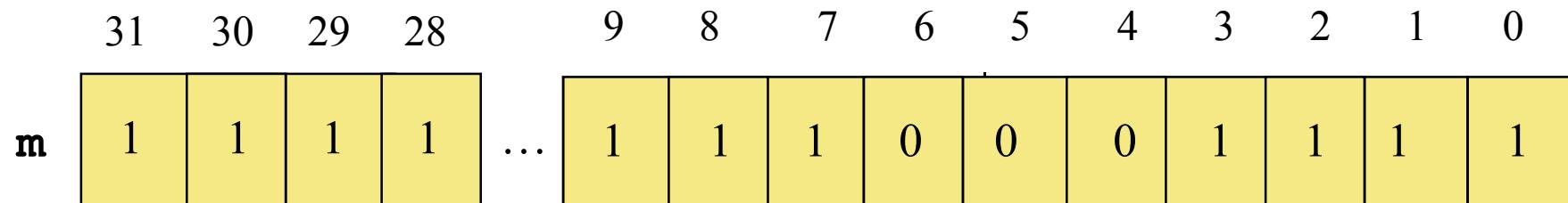
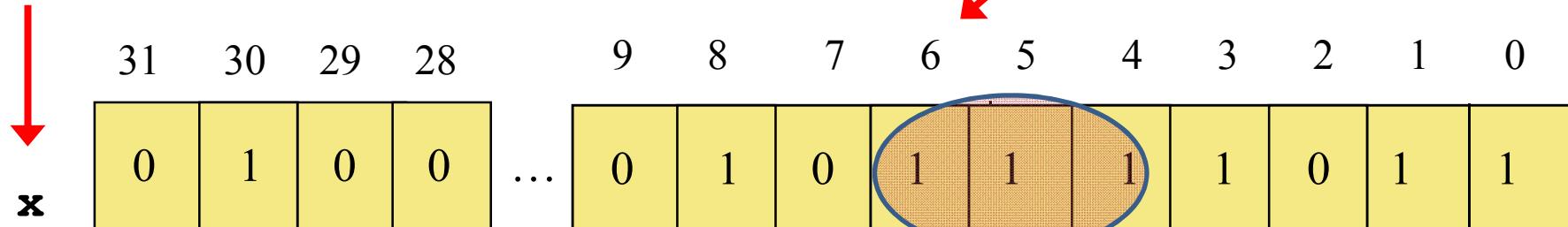


$\text{resetBits}(x, 6, 3)$

Call  $\text{resetBit}(x,p)$  in  
a loop

# Efficient resetBits(x,p,n)

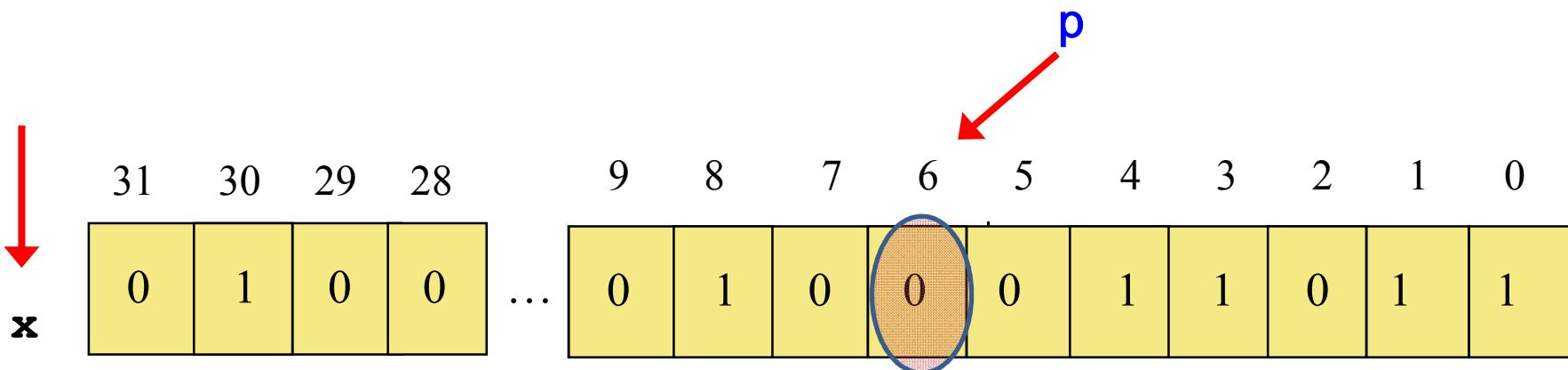
resetBits(x, 6, 3)



$x \& m$

# `invertBit(x,p)`

Write down a function `invertBit(x,p)` that will **invert** a bit of integer  $x$  at position  $p$  leaving other bits unchanged. Assume  $0 \leq p \leq 31$

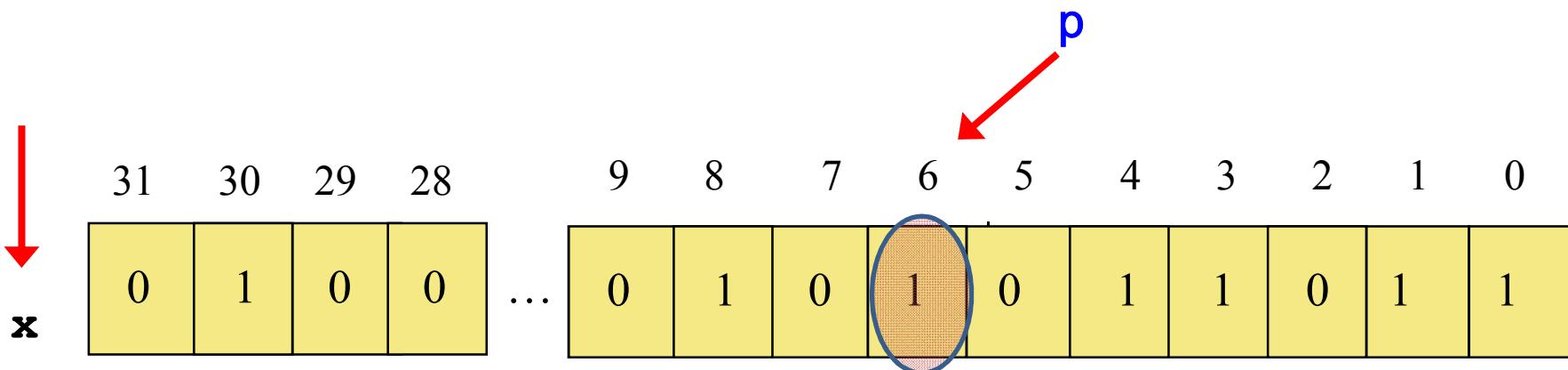


`invertBit(x, 6)`

# `invertBit(x,p)`

Write down a function `setBit(x,p)` that will **invert** a bit of integer  $x$  at position  $p$  leaving other bits unchanged.

Assume  $0 \leq p \leq 31$



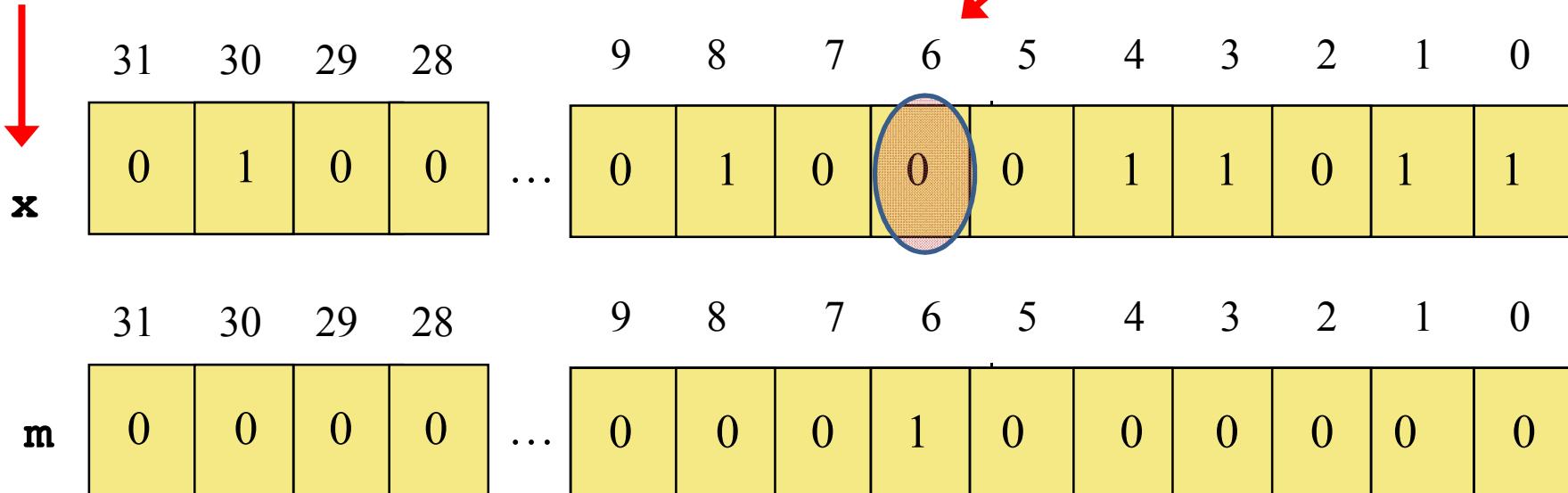
`invertBit(x, 6)`

$a \wedge 0 \rightarrow a$
$a \wedge 1 \rightarrow \sim a$
$a \wedge a \rightarrow 0$

## invertBit(x,p)

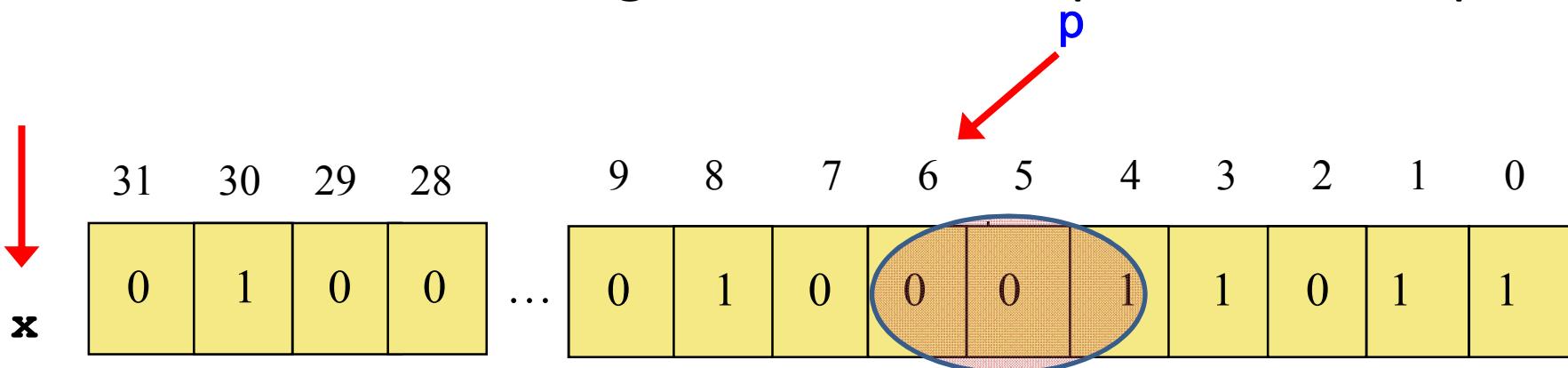
Write down a function `invertBit(x,p)` that will **invert** a bit of integer  $x$  at position  $p$  leaving other bits unchanged. Assume  $0 \leq p \leq 31$

`invertBit(x, 6)`



# invertBits(x,p,n)

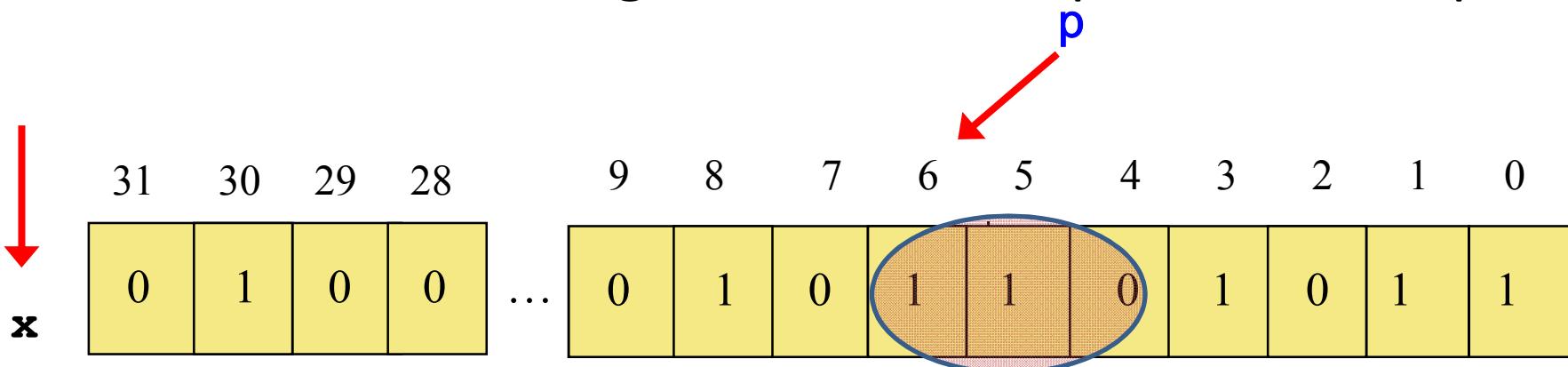
Write down a function `invertBits(x,p,n)` that will **invert** n bits of the integer x starting from position p leaving other bits unchanged. Assume  $0 \leq p \leq 31$  and  $n \leq p+1$



`invertBits(x, 6, 3)`

# invertBits(x,p,n)

Write down a function `invertBits(x,p,n)` that will **invert** n bits of the integer x starting from position p leaving other bits unchanged. Assume  $0 \leq p \leq 31$  and  $n \leq p+1$

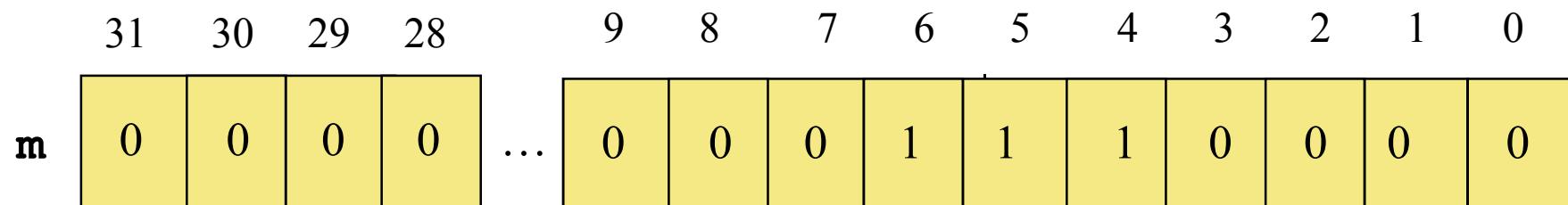
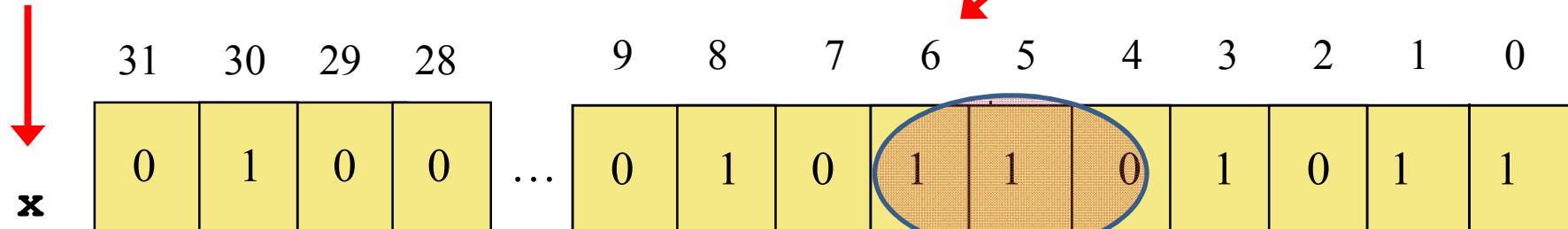


`invertBits(x, 6, 3)`

Call `invertBit(x,p)`  
in a loop

# Efficient invertBits(x,p,n)

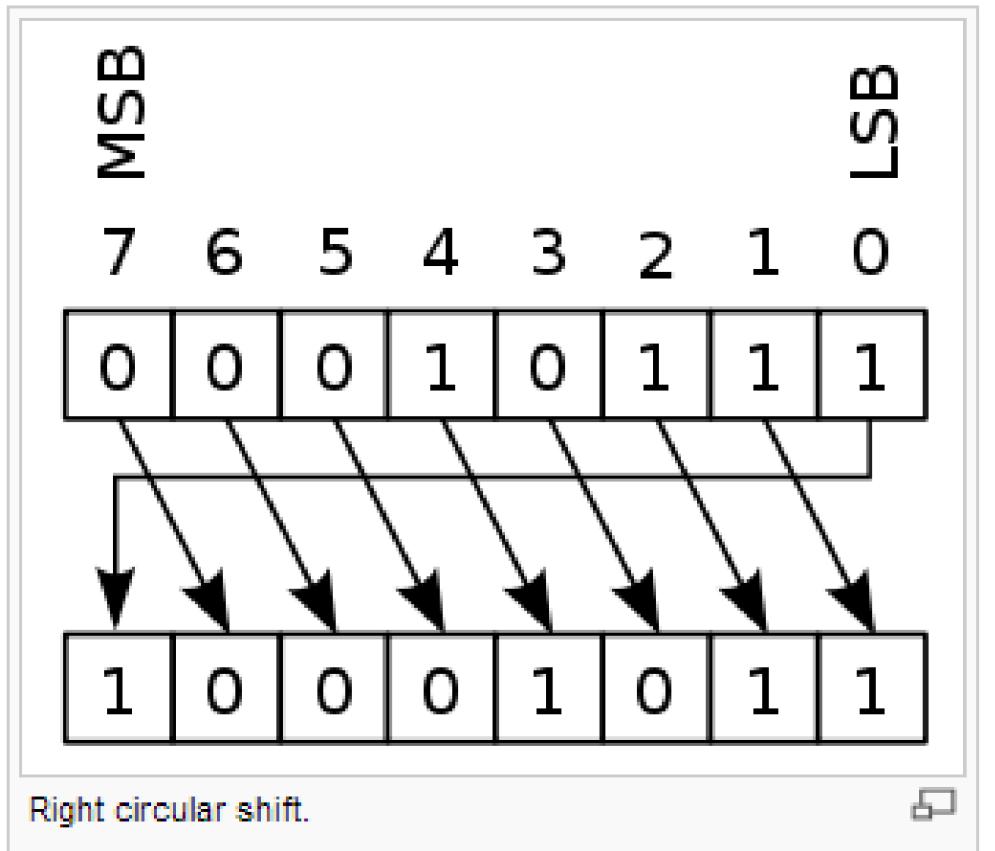
invertBits(x, 6, 3)



$x \wedge m$

# RIGHT CIRCULAR SHIFT

- to the right would yield: 1000 1011.



```
int circularRightShift(int x){  
    unsigned int y = x;  
    int s = 8*sizeof(int);  
    return (y >> 1) | x << (s-1);  
}
```

rightRotate (x, n)

# xtractRightMostBits(x,n)

Write down a function `xtractRightMostBits(x,n)` that will return rightmost  $n$  bits of the integer  $x$ .

Assume  $1 \leq n \leq 32$

